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## Lecture No. 2: Module 1: Arithmetic, Algebra and Combinatorics

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July 5, 2025

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# Indian Mathematics

Terms for the multiples of ten like 10, 20, 30 etc. in Rigveda. Terms for the higher powers of 10, given by Aryabhat, Mahaviracharya and Bhaskaracharya :

## Introduction:

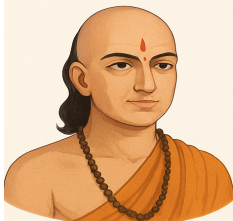
Indian mathematics is not only rich in concepts and applications but also in the linguistic and philosophical treatment of numbers. From the early Vedic texts to the classical works of Aryabhata, Mahaviracharya, and Bhaskaracharya, Indian mathematicians developed a profound understanding of numerals and place-value systems.

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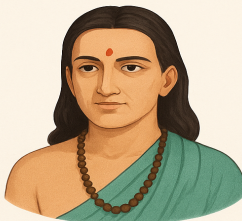
## Aryabhat, Mahaviracharya and Bhaskaracharya :



**ARYABHATA**

(c. 476–550)

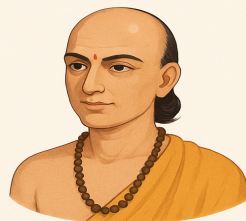
Aryabhata was an ancient Indian mathematician and astronomer. In his work 'Aryabhatiya,' he wrote about mathematics, astronomy, and the concept of zero. He introduced the place value system in India and made pioneering calculations of



**MAHAVIRA**

(c. 815–885)

Mahavira was an Indian mathematician who made significant contributions to algebra and geometry. In his major work, 'Ganitasarasamgraha,' he presented systematic rules for solving quadratic, cubic, and quartic equations.



**BHASKARACHARYA**

(c. 1114–1185)

Bhaskaracharya was a talented Indian mathematician and astronomer. His renowned works, 'Siddhanta Shiromani' and 'Lilavati,' cover topics such as algebra, arithmetic, geometry and planetary mathematics. He also made significant contributions

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Terms for the multiples of ten like 10, 20, 30 etc. in Rigveda. Terms for the higher powers of 10, given by Aryabhat, Mahaviracharya and Bhaskaracharya :

## Terms for Multiples of Ten in the Rigveda:

The **Rigveda** (composed around 1500 BCE) is one of the oldest known texts in human history and contains references to numbers and numerical systems. The Rigveda reveals that even during that early period, the decimal system and the concept of **multiples of 10** were already recognized and expressed using specific **Sanskrit terms**.

These terms show a clear decimal base and evidence of a place value system in its earliest form. Numbers were often used for describing sacrifices, poetic meters, and cosmological quantities.



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## Terms for Multiples of Ten:

Below is a list of common terms found in the Rigveda for decimal multiples:

Sanskrit Term	Modern Equivalent
Dasha	10
Dvīṃshati	20
Trīṃshat	30
Chatvāriṃshat	40
Pañchāśat	50
Shaṣṭi	60
Saptati	70
Aśīti	80
Navati	90
Shata	100



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## Higher Powers of Ten in Classical Indian Mathematics:

**a) Aryabhata (476 CE):** Aryabhata, in his work Aryabhatiya, made significant use of large numbers and had a keen understanding of the positional decimal system. He used names for powers of ten, suggesting a well-developed concept of very large numbers.

**Powers of Ten and Terms (as inferred):** Although Aryabhata didn't always name every power explicitly, his calculations and astronomical measurements involved extremely large numbers (such as the number of rotations of Earth).

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## Higher Powers of Ten in Classical Indian Mathematics:

### b) Mahaviracharya (9th century CE):

In his work "**Ganita Sara Sangraha**", Mahaviracharya provided a clear and systematic list of terms for powers of ten, which demonstrates the advanced Indian system of naming large numbers.

### Terms for Powers of Ten:

Power of 10	Sanskrit Term	Value
$10^0$	Eka	1
$10^1$	Dasha	10
$10^2$	Shata	100
$10^3$	Sahasra	1,000

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## Terms for Powers of Ten:

Power of 10	Sanskrit Term	Value
$10^4$	Ayuta	10,000
$10^5$	Laksha	100,000
$10^6$	Prayuta	1,000,000
$10^7$	Koti	10 million
$10^8$	Arbuda	100 million
$10^9$	Nyarbuda	1 billion
$10^{10}$	Samudra	10 billion
$10^{11}$	Madhya	100 billion
$10^{12}$	Antya	1 trillion
$10^{13}$	Parardha	10 trillion

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## c) Bhaskaracharya (1114–1185 CE):

Bhaskaracharya, in his celebrated work *Lilavati* and *Bijaganita*, continued the tradition of large numbers and provided many examples of calculations involving high powers of ten.

He used the same terminology established by earlier mathematicians.

In *Lilavati*, Bhaskara uses poetic language to pose problems that include very large numbers.

The positional decimal numeral system (with a placeholder zero) was extensively applied

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## Philosophical Significance:

The use of large numbers also had philosophical implications in Indian thought. Concepts such as time cycles (Kalpas) and cosmic ages (Yugas) required numerical expression that went beyond the ordinary. The need for such vast numbers encouraged the development of precise terminology.

The Rigveda provides the earliest documented use of decimal-based number naming. This system was significantly elaborated upon by later scholars like Aryabhata, Mahaviracharya, and Bhaskaracharya.

Their work laid the foundation for:

- Place-value system
- Decimal notation
- Use of zero
- Terminology for very large numbers

These contributions highlight the rich legacy of Indian mathematics, offering valuable insights into both scientific and linguistic innovations of ancient India.